

3. ∵ MNPQ 為正方形

$$\therefore M(1,4), N(2,1), P(2+\frac{x}{2}, 1+\frac{y}{2}), Q(1+\frac{x}{2}, 4+\frac{y}{2})$$

$$MN=QP=\sqrt{10}$$

$$PN=MQ=\sqrt{\left(\frac{x}{2}\right)^2 + \left(\frac{y}{2}\right)^2} = 10 \text{ (邊長相等)}$$

$$\overrightarrow{MN} \cdot \overrightarrow{PN} = 0 \text{ (四個角都直角)}$$

$$(1, -3) \cdot \left(\frac{x}{2}, \frac{y}{2}\right) = 0$$

$$\frac{x}{2} - \frac{y}{3} = 0$$

$$\begin{cases} x^2 + y^2 = 40 \\ x = 3y \end{cases}$$

$$y^2 = 4$$

$$xy = 3y^2 = 3 \times 4 = 12 \cdots (B)$$