國立羅東高級工業職業學校 () 學年度第二次教師甄試 數學 科 A

1. (4%) Let $f(x) = \frac{1}{|x|}$ and g(x) = x - 1. Find all values of x for which f(g(x)) is discontinuous.

(e) None of these

f(g(x)) is discontinuous. (a) 0 (b) 1 (c) 0,1 (d) -1,1 (e) None of these

 \bigcirc 2. (4%) Find the x-values (if any) for which f is not continuous:

 $f(x) = \begin{cases} \frac{1}{x-3} & , x \le 5\\ \frac{1}{2} & , x > 5 \end{cases}$

(a) 5 (b) $\frac{1}{2}$ (c) 3 (d) 3,5 (e) None of these

3. (4%) Find $\frac{dy}{dx}$ if $y^2 - 3xy + x^2 = 7$. (a) $\frac{2x+y}{3x-2y}$ (b) $\frac{3y-2x}{2y-3x}$ (c) $\frac{2x}{3-2y}$ (d) $\frac{2x}{y}$ (e) None of these

4. (4%) State why the Mean Value Theorem does not apply to the function $f(x) = \frac{2}{(x+1)^2}$ on the interval [-3,0].

(a) $f(-3) \neq f(0)$ (b) f is not continuous at x = -1 (c) f is not defined at x = -3 and x = 0 (d) Both (a) and (b)

5. (4%) Let f(x) be a polynomial function such that f(-2) = 5, f'(-2) = 0, and f''(-2) = 3. The point (-2,5) is a _____ the graph

of f.

(a) Relative maximum

(b) Relative minimum

(c) Intercept

(d) Point of inflection

(e) None of these

 $\begin{array}{c} 7. \ \, (4\%) \ \, \text{Evaluate} \, \int \frac{e^{\frac{1}{(x+1)^2}}}{(x+1)^2} \, dx. \\ \, \, (a) \, \frac{e^{\frac{1}{(x+1)}}}{2(x+1)} + C \quad \ \, (b) \, \frac{e^{\frac{-x}{(x+1)}}}{(x+1)^2} + C \quad \ \, (c) \, \, -e^{\frac{1}{(x+1)}} + C \quad \ \, (d) \, \frac{e^{\frac{-x}{(x+1)}}}{(x+1)^2} \\ \, \, (e) \, \, \text{None of these} \end{array}$

8. (4%) Find the sum $\sum_{n=0}^{\infty} 3(\frac{1}{2})^n$. (a) $\frac{3}{2}$ (b) 3 (c) 6 (d) $\frac{50}{9}$ (e) None of these